

AI-Augmented Algorithms – How I Learned to Stop Worrying and Love Choice

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St Andrews, 25 July 2018

Outline

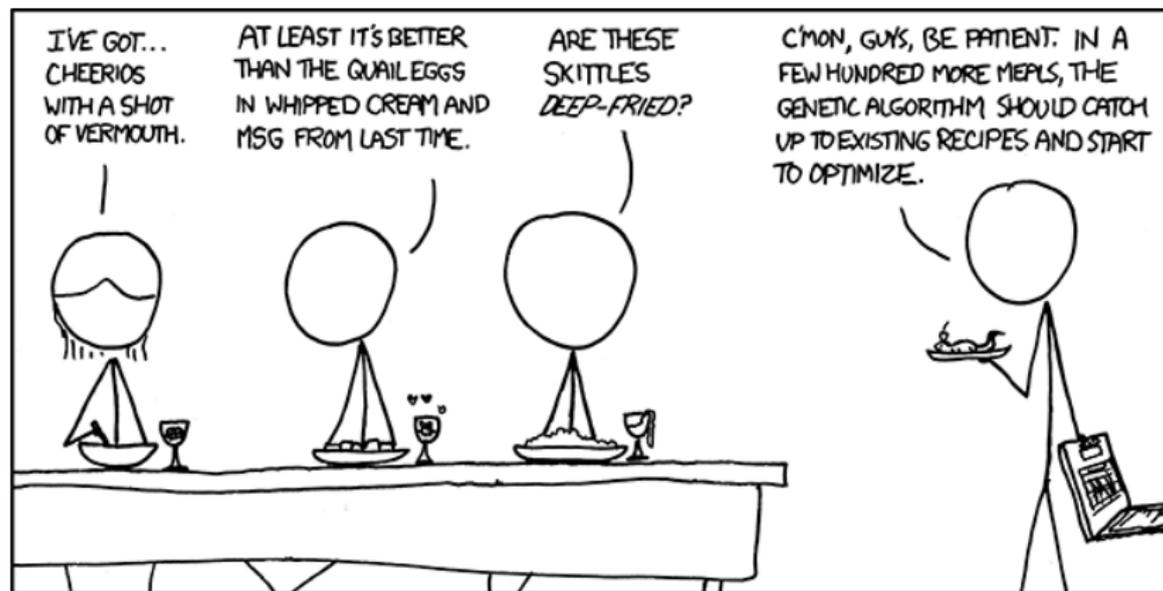
- ▷ Big Picture
- ▷ Motivation
- ▷ Algorithm Selection and Portfolios
- ▷ Algorithm Configuration
- ▷ Outlook

Big Picture

- ▷ advance the state of the art through meta-algorithmic techniques
- ▷ rather than inventing new things, use existing things more intelligently – automatically
- ▷ invent new things through combinations of existing things

Big Picture

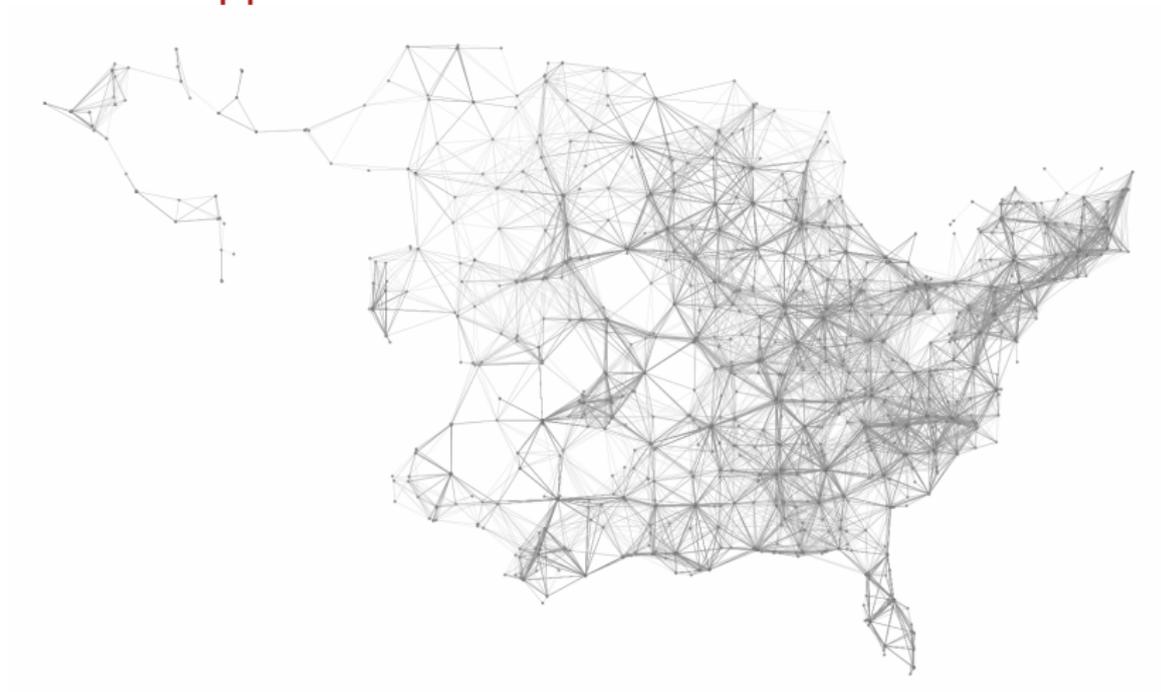
- ▷ advance the state of the art through meta-algorithmic techniques
- ▷ rather than inventing new things, use existing things more intelligently – automatically
- ▷ invent new things through combinations of existing things



WE'VE DECIDED TO DROP THE CS DEPARTMENT FROM OUR WEEKLY DINNER PARTY HOSTING ROTATION.

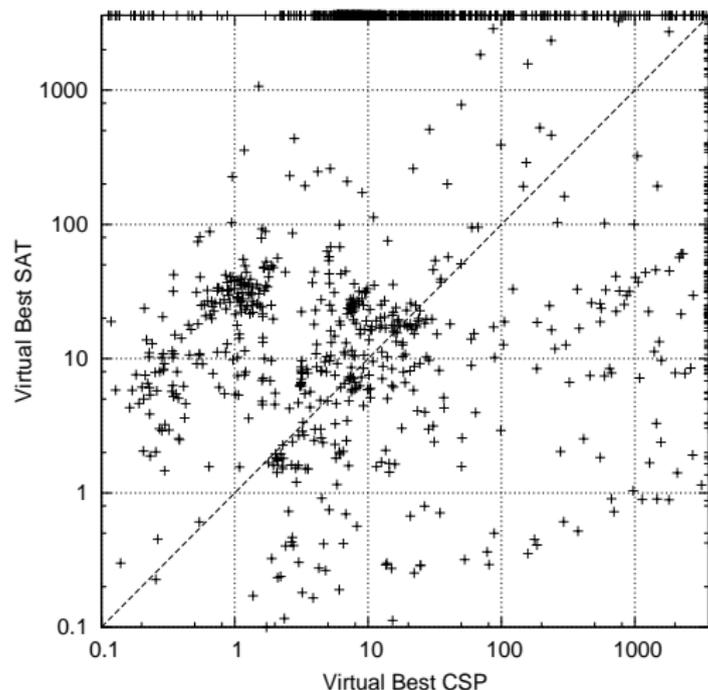
Motivation – What Difference Does It Make?

Prominent Application



Fréchette, Alexandre, Neil Newman, Kevin Leyton-Brown. "Solving the Station Packing Problem." In Association for the Advancement of Artificial Intelligence (AAAI), 2016.

Performance Differences



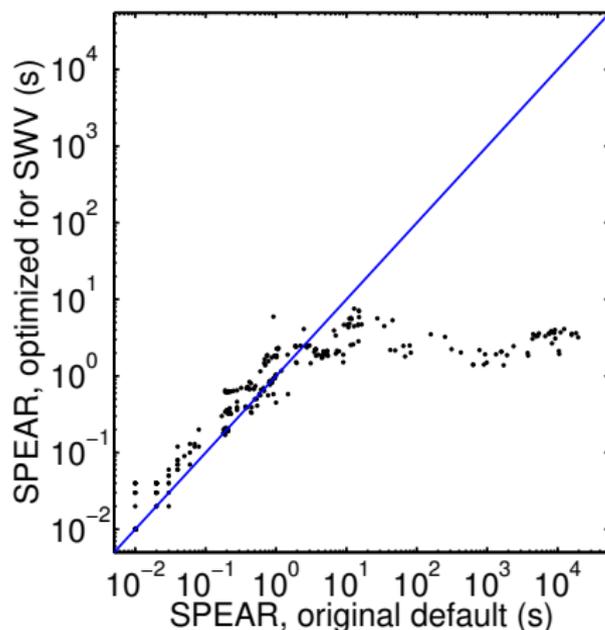
Hurley, Barry, Lars Kotthoff, Yuri Malitsky, and Barry O'Sullivan. "Proteus: A Hierarchical Portfolio of Solvers and Transformations." In CPAIOR, 2014.

Leveraging the Differences

Method	Mean PAR10	Number Solved
VB Proteus	97	1493
Proteus	1774	1424
VB CSP	3577	1349
VB SAT	17373	775
VB DirectOrder Encoding	17637	764
VB Direct Encoding	21736	593
VB Support Encoding	21986	583

Hurley, Barry, Lars Kotthoff, Yuri Malitsky, and Barry O'Sullivan. "Proteus: A Hierarchical Portfolio of Solvers and Transformations." In CPAIOR, 2014.

Performance Improvements



Hutter, Frank, Domagoj Babic, Holger H. Hoos, and Alan J. Hu. "Boosting Verification by Automatic Tuning of Decision Procedures." In FMCAD '07: Proceedings of the Formal Methods in Computer Aided Design, 27–34. Washington, DC, USA: IEEE Computer Society, 2007.

Common Theme

Performance models of black-box processes

- ▷ also called surrogate models
- ▷ replace expensive underlying process with cheap approximate model
- ▷ build approximate model based on real evaluations using machine learning techniques
- ▷ no knowledge of what the underlying process does required (but can be helpful)
- ▷ allow better understanding of the underlying process through interrogation of the model

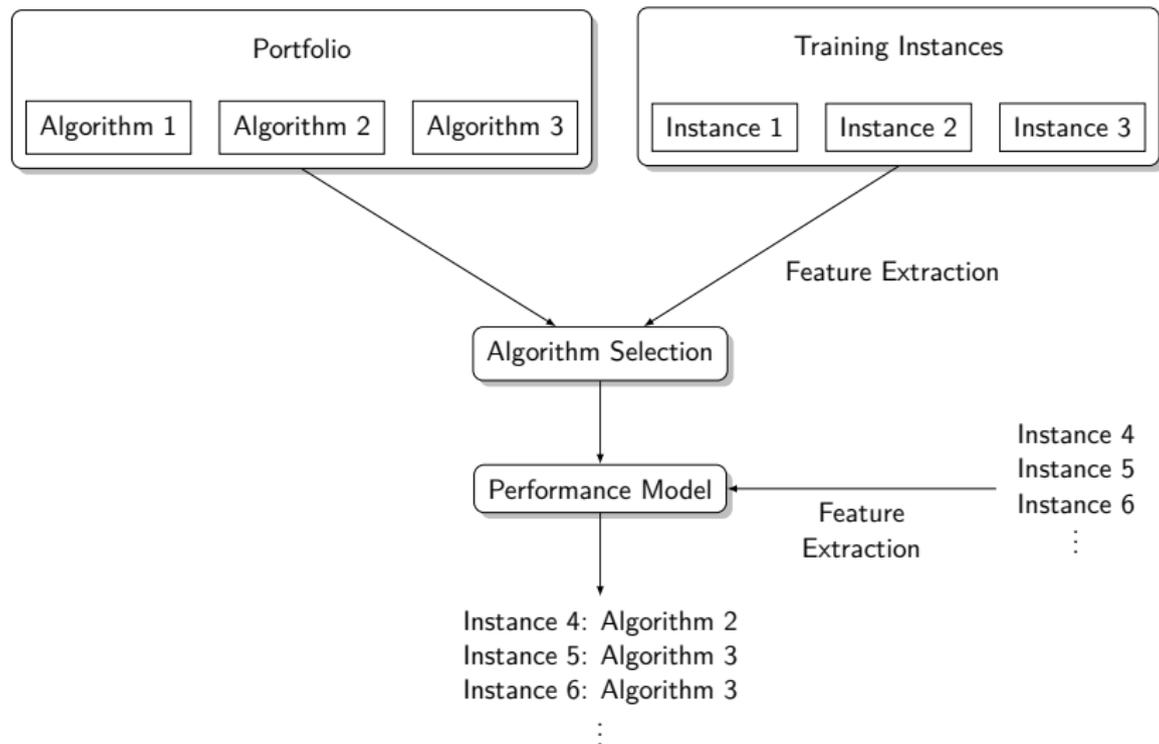
Algorithm Selection

Algorithm Selection

Given a problem, choose the best algorithm to solve it.

Rice, John R. "The Algorithm Selection Problem." *Advances in Computers* 15 (1976): 65–118.

Algorithm Selection



Algorithm Portfolios

- ▷ instead of a single algorithm, use several complementary algorithms
- ▷ idea from Economics – minimise risk by spreading it out across several securities
- ▷ same for computational problems – minimise risk of algorithm performing poorly
- ▷ in practice often constructed from competition winners

Huberman, Bernardo A., Rajan M. Lukose, and Tad Hogg. "An Economics Approach to Hard Computational Problems." *Science* 275, no. 5296 (1997): 51–54. doi:10.1126/science.275.5296.51.

Algorithms

“algorithm” used in a very loose sense

- ▷ algorithms
- ▷ heuristics
- ▷ machine learning models
- ▷ consistency levels
- ▷ ...

Parallel Portfolios

Why not simply run all algorithms in parallel?

- ▷ not enough resources may be available/waste of resources
- ▷ algorithms may be parallelized themselves
- ▷ memory contention

Building an Algorithm Selection System

- ▷ most approaches rely on machine learning
- ▷ train with representative data, i.e. performance of all algorithms in portfolio on a number of instances
- ▷ evaluate performance on separate set of instances
- ▷ potentially large amount of prep work

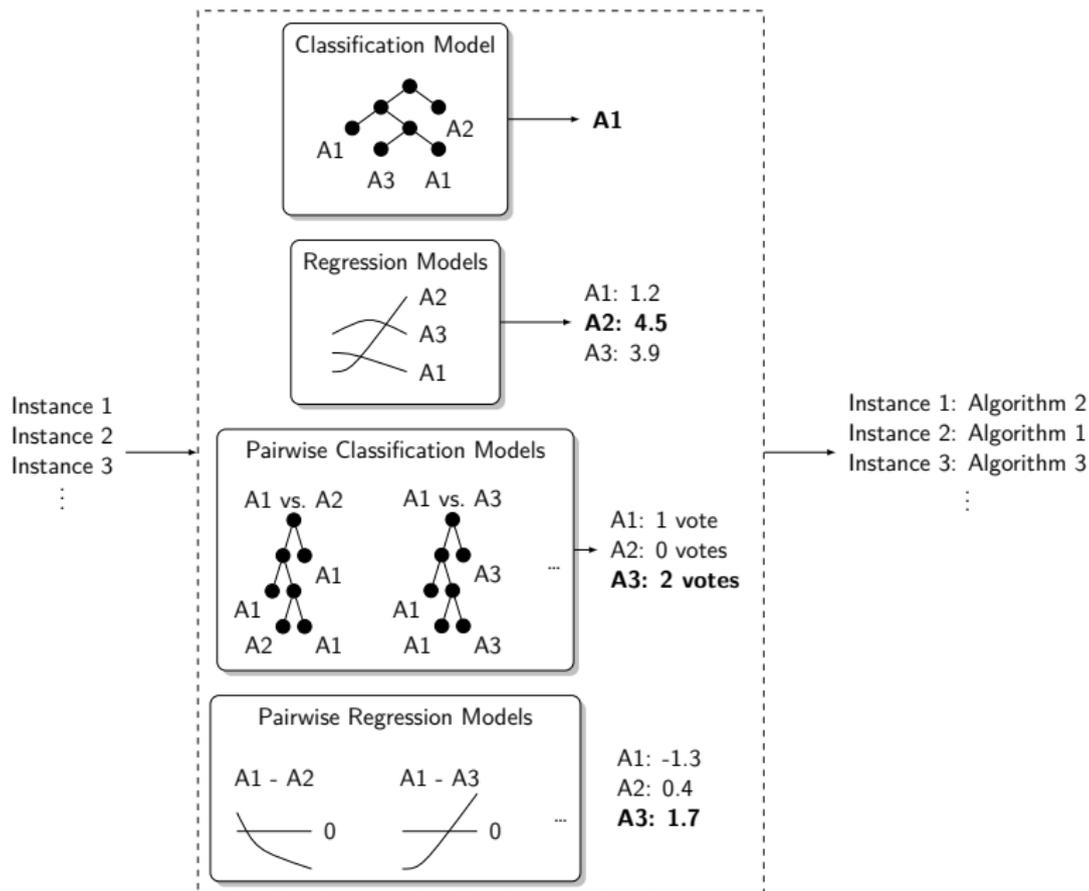
Key Components of an Algorithm Selection System

- ▷ feature extraction
- ▷ performance model
- ▷ prediction-based selector/scheduler

optional:

- ▷ presolver
- ▷ secondary/hierarchical models and predictors (e.g. for feature extraction time)

Types of Performance Models



Benchmark Library – ASlib

- ▷ currently 29 data sets/scenarios with more in preparation
- ▷ SAT, CSP, QBF, ASP, MAXSAT, OR, machine learning...
- ▷ includes data used frequently in the literature that you may want to evaluate your approach on
- ▷ performance of common approaches that you can compare to
- ▷ <http://aslib.net>

Bischi, Bernd, Pascal Kerschke, Lars Kotthoff, Marius Lindauer, Yuri Malitsky, Alexandre Fréchet, Holger H. Hoos, et al. "ASlib: A Benchmark Library for Algorithm Selection." *Artificial Intelligence Journal (AIJ)*, no. 237 (2016): 41–58.

(Much) More Information

Comments? Suggestions? Corrections?
lars.kotthoff

Algorithm Selection literature summary

Last update 16 February 2018

click headings to sort
click columns to expand



citation	domain	features	predict what	predict how	predict when	portfolio	year
Langley 1983a, Langley 1983b	search	past performance	algorithm	hand-crafted and learned rules	offline and online	dynamic	1983
Carbonei et al. 1991	planning	problem domain features, search statistics	control rules	explanation-based rule construction	offline	dynamic	1991
Gratch and DeJong 1992	planning	problem domain features, search statistics	control rules	probabilistic rule construction	online	dynamic	1992
Smith and Sabelf 1992	software design	features of abstract representation	algorithms and data structures	simulated annealing	offline	static	1992
Aho 1992	machine learning	instance features	algorithm	learned rules	offline	static	1992
Brosley 1993	machine learning	instance and algorithm features	algorithm	hand-crafted rules	offline	static	1993
Karrel et al. 1993	differential equations	past performance, instance features	algorithm	hand-crafted rules	offline	static	1993
Minton 1993a, Minton 1993b, Minton 1994	constraints	runtime performance	algorithm	hand-crafted and learned rules	offline	dynamic	1993
Cahil 1994	software design	instance features	algorithms and data structures	frame-based knowledge base	offline	static	1994
Tsang et al. 1995	constraints	instance features	algorithm	-	-	static	1995
Brewer 1995	software design	runtime performance	algorithms, data structures and their parameters	statistical model	offline	static	1995
Wierawakana et al. 1996, Joehi et al. 1996	differential equations	instance features	runtime performance	Bayesian belief propagation, neural nets	offline	static	1996
Bornet et al. 1996	constraints	search statistics	switch algorithm?	hand-crafted rules	online	static, static order	1996
Allen and Minton 1996	SAT, constraints	probing	runtime performance	hand-crafted rules	offline	static	1996
Sakkout et al. 1996	constraints	search statistics	switch algorithm?	hand-crafted rules	online	static	1996
Huerman et al. 1997	graph colouring	past performance	resource allocation	statistical model	offline	static	1997
Gomes and Selman 1997a, Gomes and Selman 1997b	constraints	problem size and past performance	algorithm	statistical model	offline	static	1997
Cook and Vareel 1997	parallel search	probing	set of search strategies	decision trees, Bayesian classifier, nearest neighbour, neural net	online	static	1997
Finz 1997, Finz 1998	planning	past performance	resource allocation	statistical model, regression	offline	static	1997
Lofton and Larshoff 1998	branch and bound	probing	runtime performance	hand-crafted rules	online	static	1998
Casseu et al. 1999	vehicle routing problem	runtime performance	algorithm	genetic algorithms	offline	static	1999
Howe et al. 1999	planning	instance features	resource allocation	linear regression	offline	static	1999
Teschiera-Marin et al. 1999	scheduling	instance and search features	algorithm	genetic algorithms	offline	dynamic	1999
Wilson et al. 2000	software design	instance features	data structures	nearest neighbour	offline	static	2000
Beck and Fox 2000	job shop scheduling	instance feature changes during search	algorithm scheduling policy	hand-crafted rules	offline	static	2000
Brazdil and Soares 2000	classification	past performance	instans	distribution model	offline	static	2000
Lapoutnik and Litman 2000	order selection, sorting	instance features	remaining cost for each sub-problem	MDP	offline	static	2000
Sillis 2000	constraints	probing	cost of solving problem	statistical model	offline	static	2000
Phylringer et al. 2000	classification	instance features, probing	algorithm	9 different classifiers	offline	static	2000
Fukunaga 2000	TSP	past performance	resource allocation	performance simulation for different allocations	offline	static	2000
Soares and Brazdil 2000	machine learning	instance features	instans	nearest neighbour	offline	static	2000
Gomes and Selman 2001	constraints, mixed integer programming	past performance	algorithm	statistical model	offline	dynamic	2001
Epstein and Fleuder 2001, Epstein et al. 2002, Epstein et al. 2005, Epstein and Petrovic 2011	constraints	variable characteristics	algorithm	weights, hand-crafted rules	offline and online	dynamic	2001
Lapoutnik and Litman 2001	DPLL branching rules	instance features	remaining cost for each sub-problem	MDP	offline	static	2001
Naryayk 2001	optimization	search statistics	expected utility of algorithm	reinforcement learning	offline and online	static	2001
Horvitz et al. 2001	constraints	instance and instance generator features, search statistics	runtime performance, restart parameters	Bayesian model	offline and online	static	2001
Bornet and Tsang 2001	constraints	instance features, search	redundant constraints to add	hand-crafted rules	offline	-	2001

<http://larskotthoff.github.io/assurvey/>

Kotthoff, Lars. "Algorithm Selection for Combinatorial Search Problems: A Survey." *AI Magazine* 35, no. 3 (2014): 48–60.

Algorithm Configuration

Algorithm Configuration

Given a (set of) problem(s), find the best parameter configuration.

Parameters?

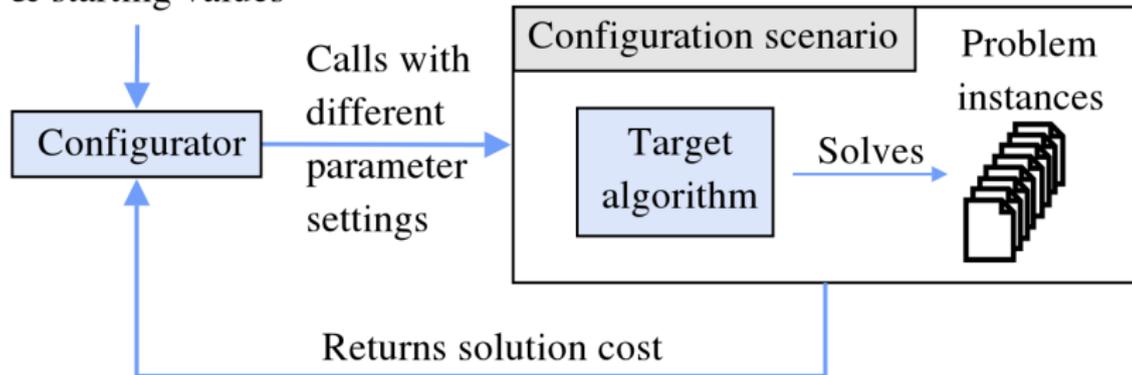
- ▷ anything you can change that makes sense to change
- ▷ e.g. search heuristic, variable ordering, type of global constraint decomposition
- ▷ **not** random seed, whether to enable debugging, etc.
- ▷ some will affect performance, others will have no effect at all

Automated Algorithm Configuration

- ▷ no background knowledge on parameters or algorithm
- ▷ as little manual intervention as possible
 - ▷ failures are handled appropriately
 - ▷ resources are not wasted
 - ▷ can run unattended on large-scale compute infrastructure

Algorithm Configuration

Parameter domains
& starting values



Frank Hutter and Marius Lindauer, "Algorithm Configuration: A Hands on Tutorial", AAAI 2016

General Approach

- ▷ evaluate algorithm as black box function
- ▷ observe effect of parameters without knowing the inner workings
- ▷ decide where to evaluate next
- ▷ balance diversification/exploration and intensification/exploitation

When are we done?

- ▷ most approaches incomplete
 - ▷ cannot prove optimality, not guaranteed to find optimal solution (with finite time)
 - ▷ performance highly dependent on configuration space
- How do we know when to stop?

Time Budget

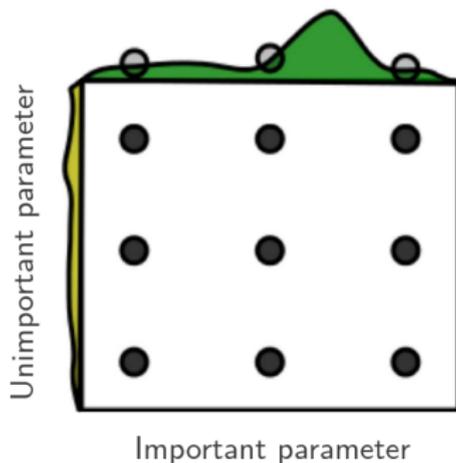
How much time/how many function evaluations?

- ▷ too much → wasted resources
- ▷ too little → suboptimal result
- ▷ use statistical tests
- ▷ evaluate on parts of the instance set
- ▷ for runtime: adaptive capping

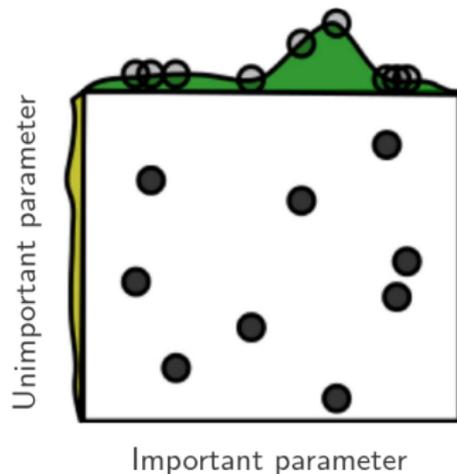
Grid and Random Search

- ▷ evaluate certain points in parameter space

Grid Layout



Random Layout



Bergstra, James, and Yoshua Bengio. "Random Search for Hyper-Parameter Optimization." *J. Mach. Learn. Res.* 13, no. 1 (February 2012): 281–305.

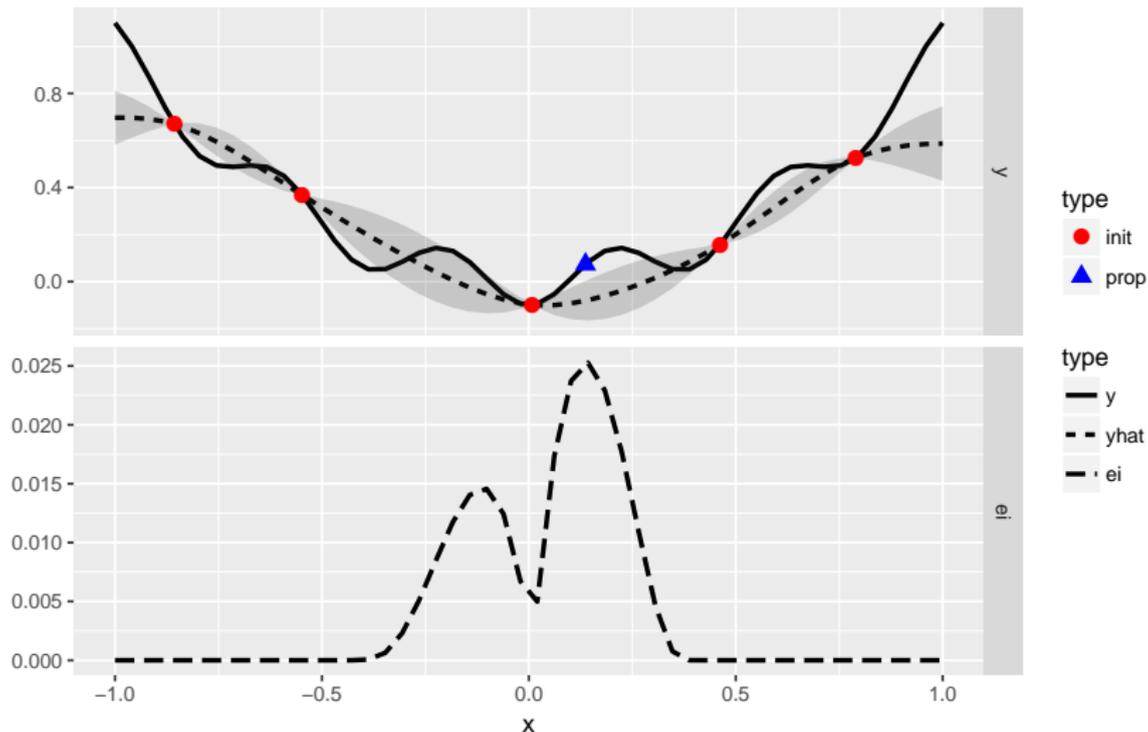
Model-Based Search

- ▷ evaluate small number of configurations
- ▷ build model of parameter-performance surface based on the results
- ▷ use model to predict where to evaluate next
- ▷ repeat
- ▷ allows targeted exploration of new configurations
- ▷ can take instance features into account like algorithm selection

Hutter, Frank, Holger H. Hoos, and Kevin Leyton-Brown. "Sequential Model-Based Optimization for General Algorithm Configuration." In LION 5, 507–23, 2011.

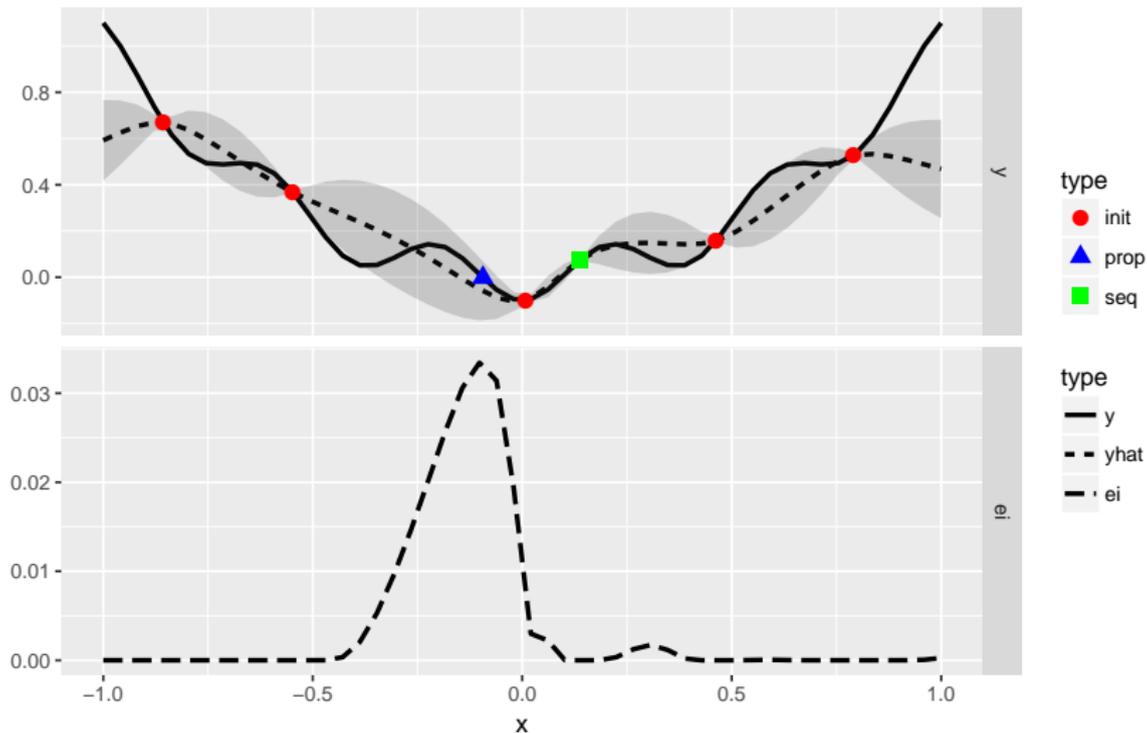
Model-Based Search Example

Iter = 1, Gap = 1.9909e-01



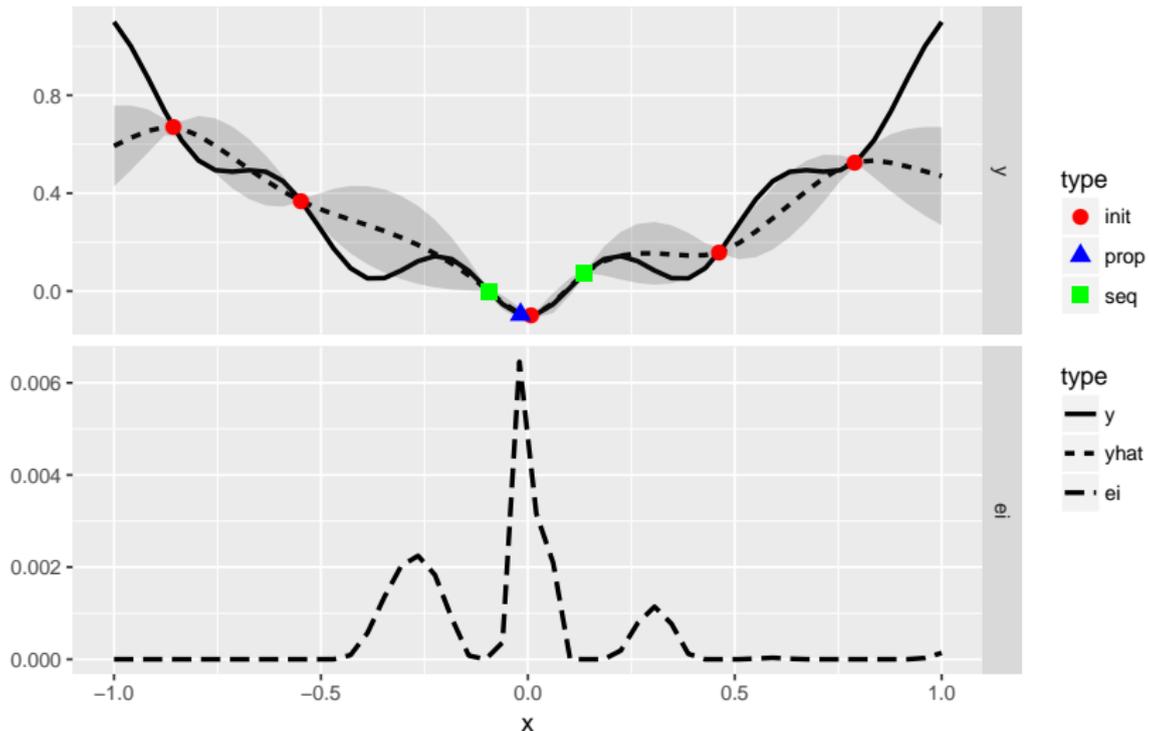
Model-Based Search Example

Iter = 2, Gap = 1.9909e-01



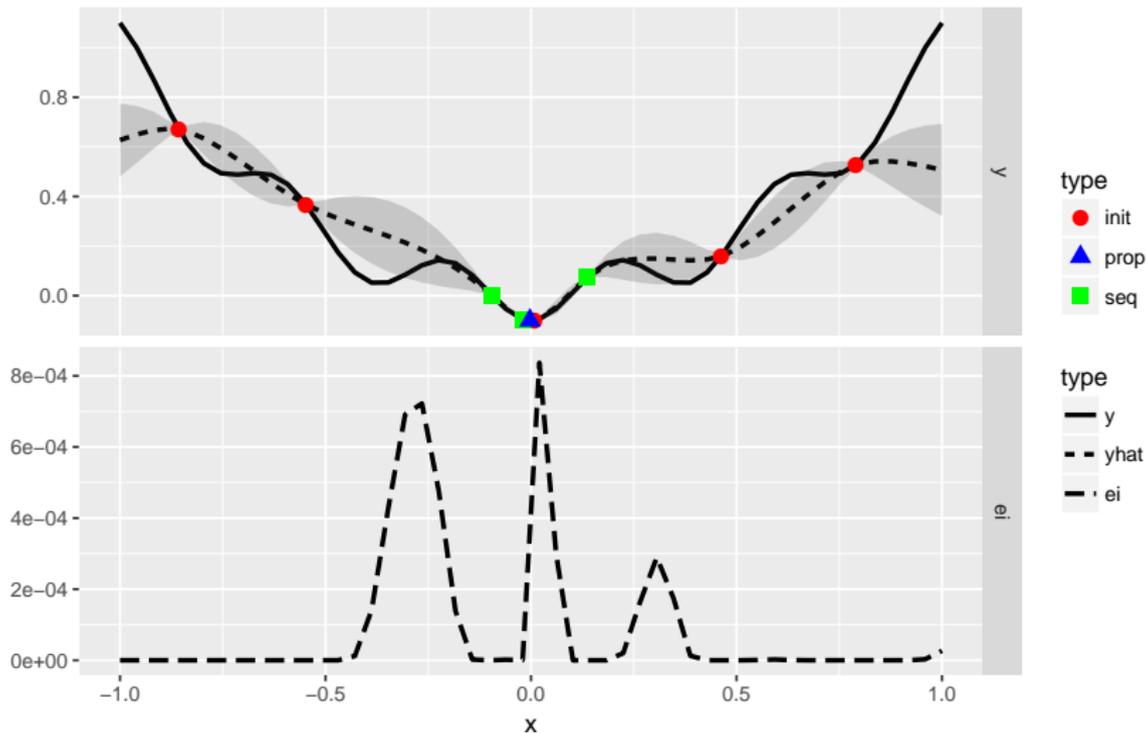
Model-Based Search Example

Iter = 3, Gap = 1.9909e-01



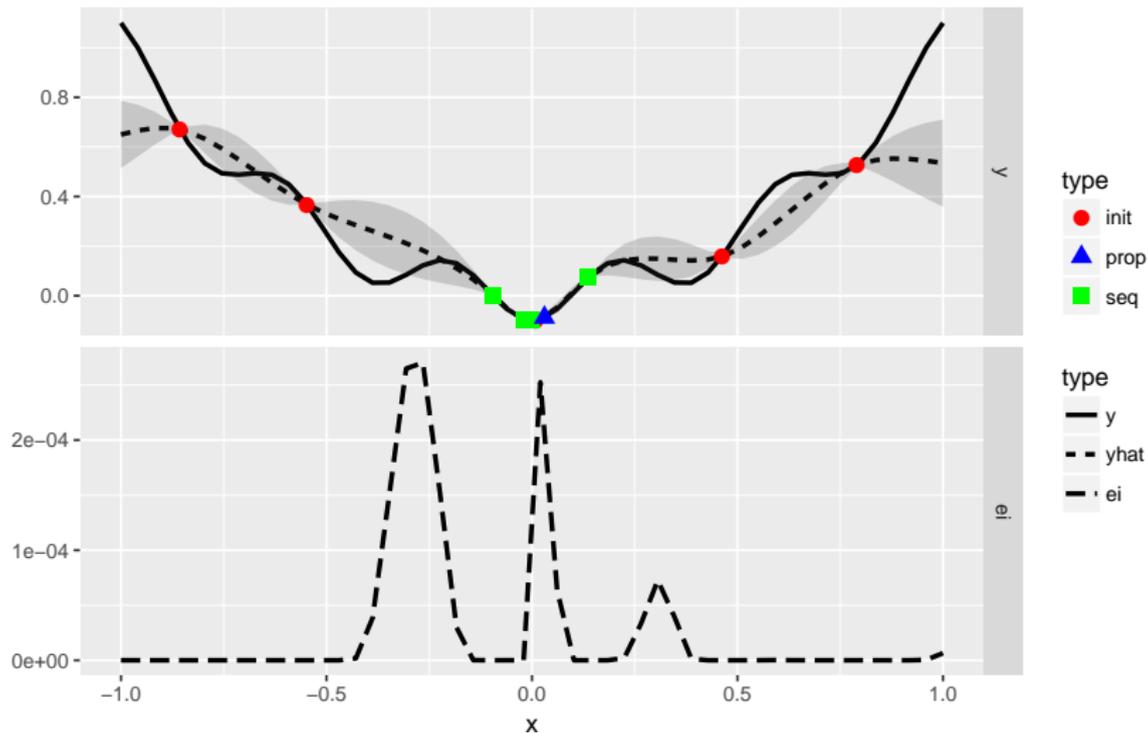
Model-Based Search Example

Iter = 4, Gap = 1.9992e-01



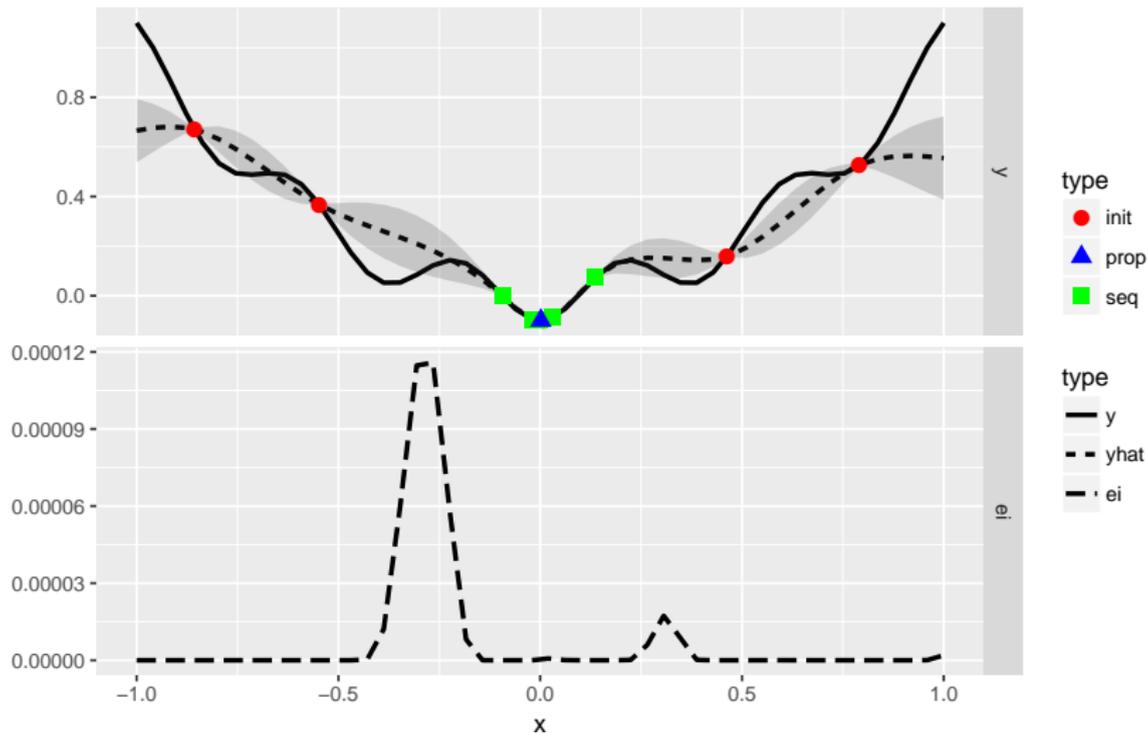
Model-Based Search Example

Iter = 5, Gap = 1.9992e-01



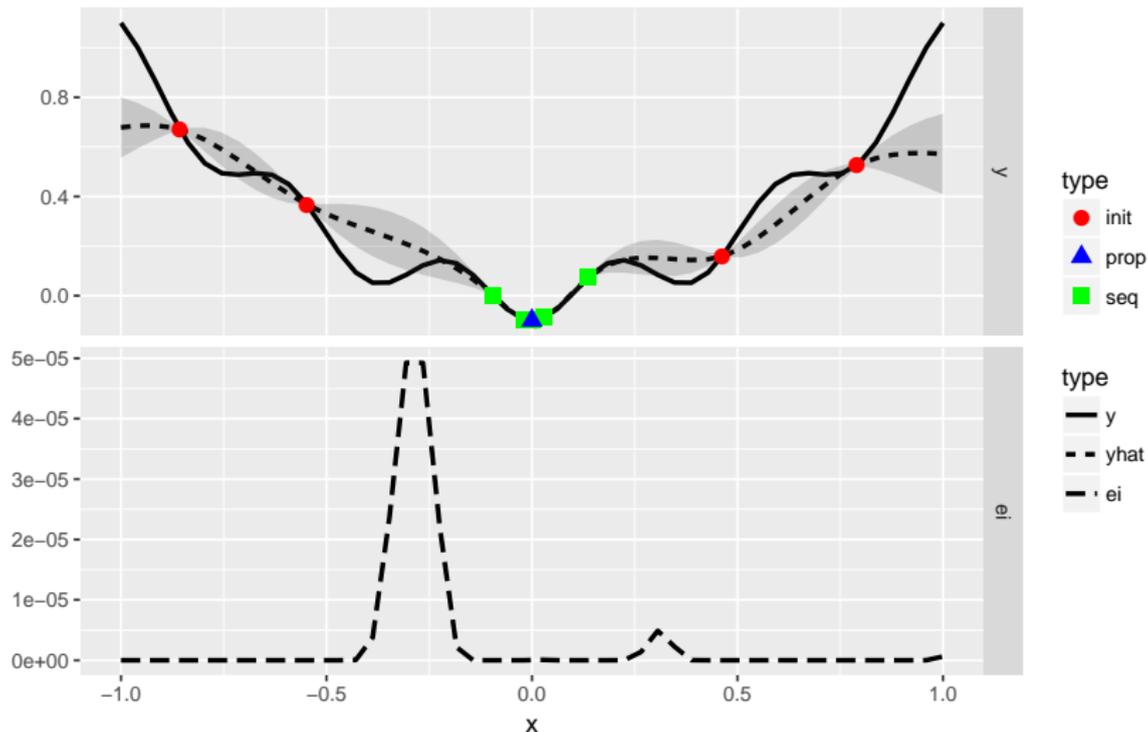
Model-Based Search Example

Iter = 6, Gap = 1.9996e-01



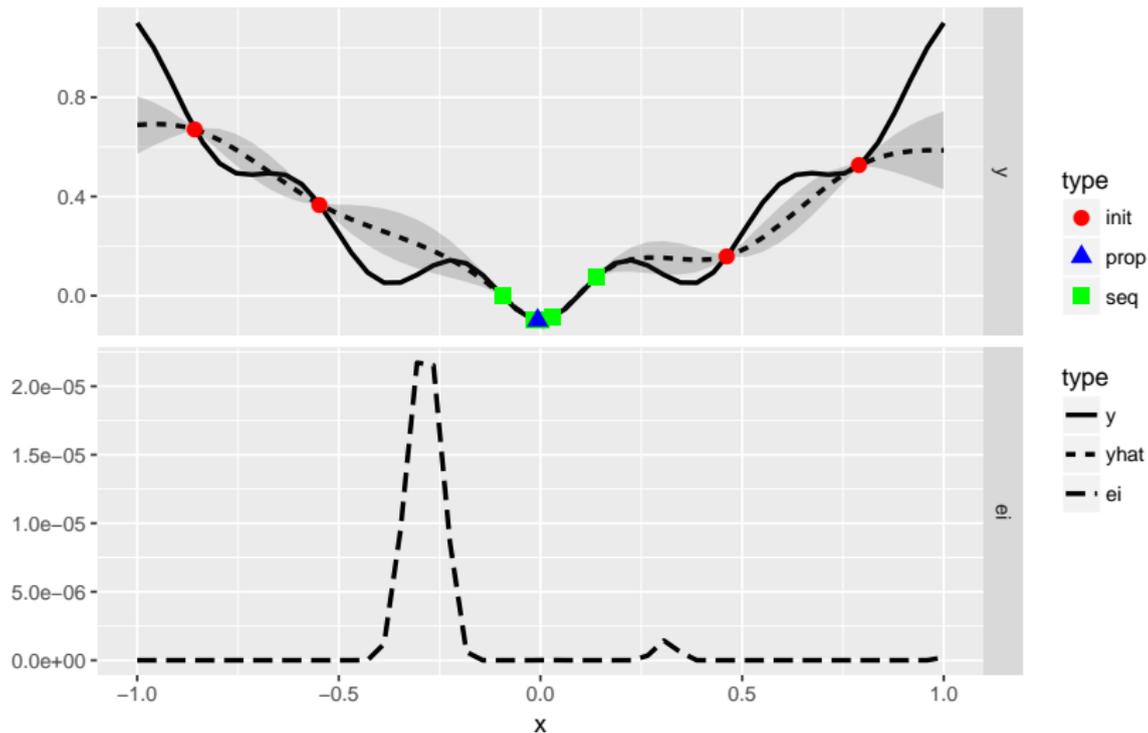
Model-Based Search Example

Iter = 7, Gap = 2.0000e-01



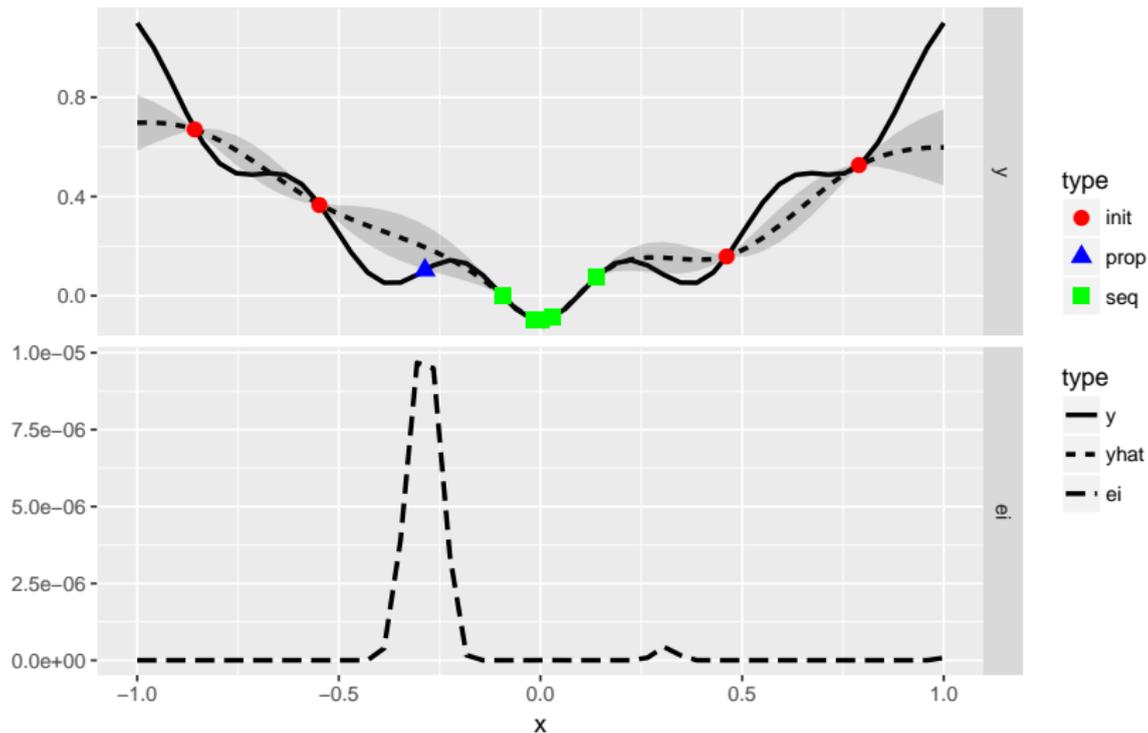
Model-Based Search Example

Iter = 8, Gap = 2.0000e-01



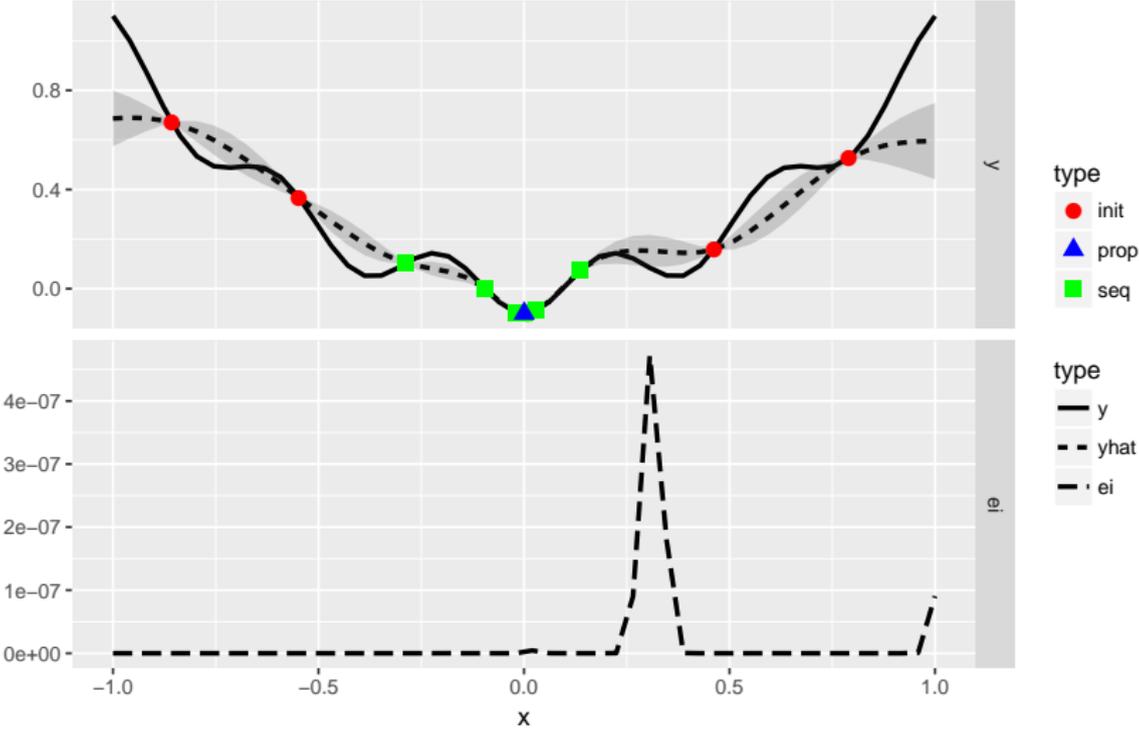
Model-Based Search Example

Iter = 9, Gap = 2.0000e-01



Model-Based Search Example

Iter = 10, Gap = 2.0000e-01



Benchmark Library – AClib

- ▷ ASP, MIP, planning, machine learning, ...
- ▷ 4 algorithm configuration tools from the literature already integrated
- ▷ <https://bitbucket.org/mlindauer/aclib2>

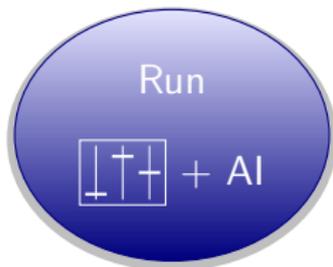
Hutter, Frank, Manuel López-Ibáñez, Chris Fawcett, Marius Lindauer, Holger H. Hoos, Kevin Leyton-Brown, and Thomas Stützle. “AClib: A Benchmark Library for Algorithm Configuration.” In *Learning and Intelligent Optimization*, 36–40. Cham: Springer International Publishing, 2014.

Outlook

Quo Vadis, Software Engineering?



Quo Vadis, Software Engineering?



Hoos, Holger H. "Programming by Optimization." Communications of the Association for Computing Machinery (CACM) 55, no. 2 (February 2012): 70–80. <https://doi.org/10.1145/2076450.2076469>.

Meta-Algorithmics in the Physical Realm – AI and Lasers



Tools and Resources

LLAMA <https://bitbucket.org/lkotthoff/llama>

SATzilla <http://www.cs.ubc.ca/labs/beta/Projects/SATzilla/>

iRace <http://iridia.ulb.ac.be/irace/>

mlrMBO <https://github.com/mlr-org/mlrMBO>

SMAC <http://www.cs.ubc.ca/labs/beta/Projects/SMAC/>

Spearmint <https://github.com/HIPS/Spearmint>

TPE <https://jaberg.github.io/hyperopt/>

autofolio <https://bitbucket.org/mlindauer/autofolio/>

Auto-WEKA <http://www.cs.ubc.ca/labs/beta/Projects/autoweeka/>

Auto-sklearn <https://github.com/automl/auto-sklearn>

Summary

Algorithm Selection choose the best *algorithm* for solving a problem

Algorithm Configuration choose the best *parameter configuration* for solving a problem with an algorithm

- ▷ mature research areas
- ▷ can combine configuration and selection
- ▷ effective tools are available
- ▷ COnfiguration and SElection of ALgorithms group COSEAL
<http://www.coseal.net>

Don't set parameters prematurely, embrace choice!

I'm hiring!



Several funded graduate positions available.

